Week 68 (12/29/03) Tower of circles

Consider N circles stacked on top of each other inside an isosceles triangle, as shown below for the case N = 4. Let A_C be the sum of the areas of the N circles, and let A_T be the area of the triangle. In terms of N, what should the vertex angle, α , be so that the ratio A_C/A_T is maximized? Assume that N is large, and ignore terms in your answer that are of subleading order in N.

