The brachistochrone

A bead is released from rest at the origin and slides down a frictionless wire that connects the origin to a given point, as shown. What shape should the wire take so that the bead reaches the endpoint in the shortest possible time?

